

13.5

$$\frac{-x-3}{x+2}$$

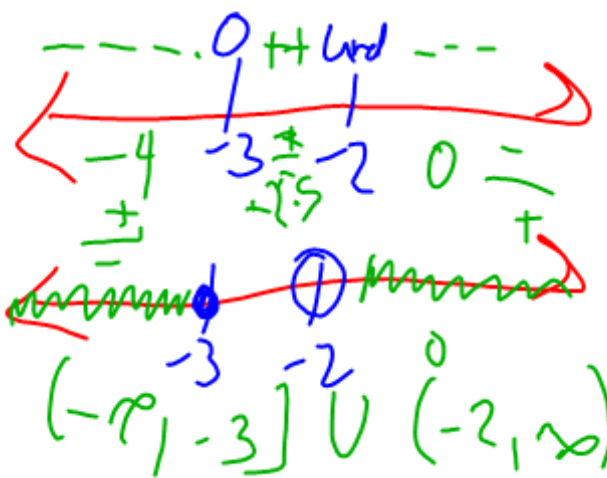
$$\leq 0$$

vs

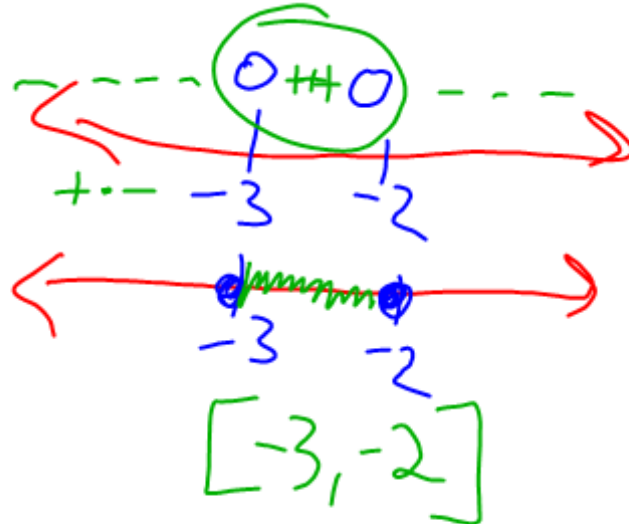
$$(-x-3)(x+2) \geq 0$$

Zeros: $x = -3$
 $x = -2$

$x = -3$ zero } critical
 $x \neq -2$ undef } #



intervals
 $(-\infty, -3)$
 $(-3, -2)$
 $(-2, \infty)$



$$[-3, -2]$$

13.4

ate substitution. When necessary, check prop

$$21. (2x - 5)^2 + 4(2x - 5) + 3 = 0$$

Solve using u-substitution

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$$\text{let } u = 2x - 5$$

$$u^2 + 4u + 3 = 0$$

$$(u + 3)(u + 1) = 0$$

$$u = -3 \quad u = -1$$

$$u = -3$$

$$2x - 5 = -3$$

$$2x = 2$$

$$x = 1$$

$$u = -1$$

$$2x - 5 = -1$$

$$2x = 4$$

$$x = 2$$

13.1 Solving Quadratics

1) Factoring

2) Completing the Square

13.2 → 3) Quadratic Formula



13.1 Solve

$$\frac{5(x+1)^2}{5} = \frac{10}{5}$$

$$\sqrt{(x+1)^2} = \pm\sqrt{2}$$

$$x+1 = \pm\sqrt{2}$$

$$x = -1 \pm\sqrt{2}$$

Solve
By 2 Completing the Square

$$x^2 + 3x + 4 = 0$$

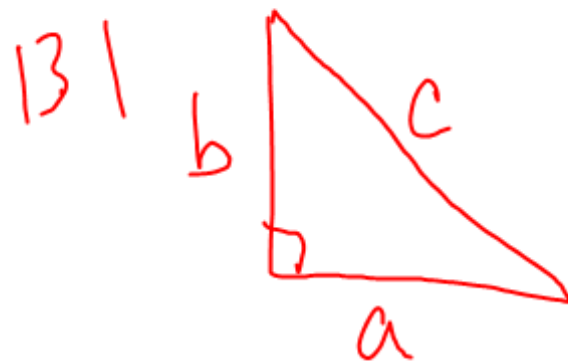
$$x^2 + 3x + \frac{9}{4} = -4 + \frac{9}{4}$$

$$\frac{1}{2}\left(\frac{3}{1}\right) = \left(\frac{3}{2}\right)$$

$$\sqrt{\left(x + \frac{3}{2}\right)^2} = \pm\sqrt{-\frac{7}{4}}$$

$$x + \frac{3}{2} = \frac{\pm\sqrt{7}i}{2}$$

$$x = -\frac{3}{2} \pm \frac{\sqrt{7}}{2}i$$



$$a^2 + b^2 = c^2$$

13.2

$$X = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

vertex Formula

discriminant

$$b^2 - 4ac$$

$$2^2 = 4(3)(-1)$$

$$16$$

Solve $3x^2 + 2x - 1 = 0$ use Q.F.

$$X = \frac{-(2) \pm \sqrt{2^2 - 4(3)(-1)}}{2(3)} = \frac{-2 \pm \sqrt{16}}{6} = \frac{-2 \pm 4}{6}$$

$\rightarrow \frac{-1}{3}$
 $\rightarrow \frac{1}{3}$

determine the # and type of solutions

1 or 2 Real complex

$$4x^2 - 10x - 2 = 0$$

$$b^2 - 4ac = (-10)^2 - 4(4)(-2)$$

$$= 100 + 32$$

$$= 132$$

2 irrational solutions

Ration. irrat.
Real

Graphing133

$$y = x^2 - 2x - 8$$

① find the vertex

$$y + 8 + 1 = x^2 - 2x + 1$$

$$y + 9 = (x - 1)^2$$

$$y = (x - 1)^2 - 9$$

Complete the
square to
write in
Vertex form

$$y = a(x - h)^2 + k$$

$v(1, -9)$ min

$$y = (x-1)^2 - 9$$

v $\textcircled{1}$ $(1, -9)$ $\textcircled{2}$ min
 $x=1$

X-intercepts

let $y=0$

$$0 = (x-1)^2 - 9$$

$$\pm\sqrt{9} = \sqrt{(x-1)^2}$$

$$\pm 3 = x - 1$$

$$\pm 3 = x$$

$$x = 4, -2$$

y-intercept

let $x=0$

$$y = (-1)^2 - 9$$

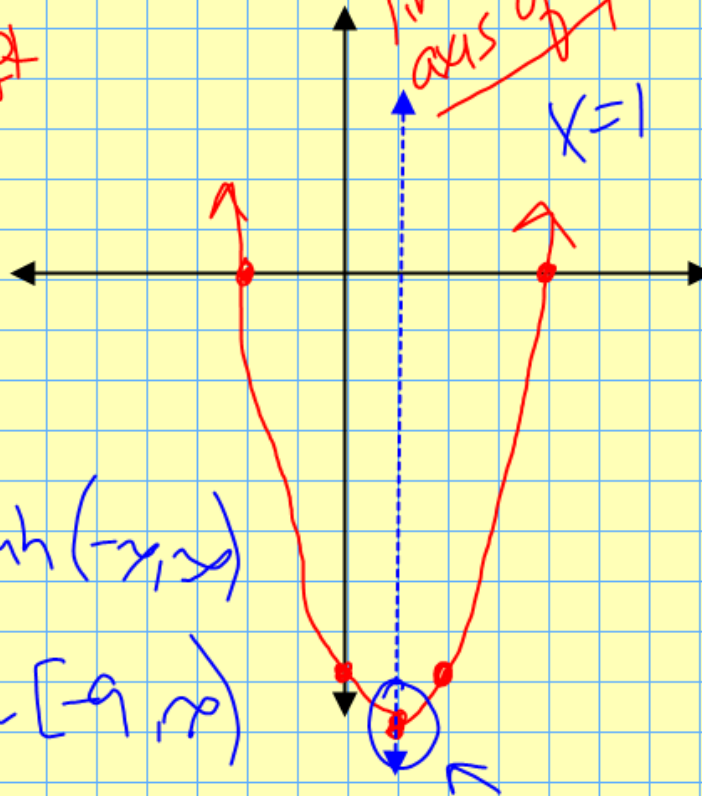
$$y = -8$$

Domain $(-\infty, \infty)$

Range $[-9, \infty)$

line axis of symmetry

$$x=1$$



$$17. f(x) = x^2 - 2x - 5$$

A baseball player hits a pop fly into the air. The function

$$s(t) = -16t^2 + 64t + 5$$

models the ball's height above the ground, $s(t)$, in feet, t seconds after it is hit. Use the function to solve Exercises 18–19.

18. When does the baseball reach its maximum height? What is that height?

19. After how many seconds does the baseball hit the ground?

Round to the nearest tenth of a second.



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18. When does the baseball reach its maximum height? What is that height?

$t = \text{time}$
 $s(t) = \text{height}$
 above ground

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Vertex Formula

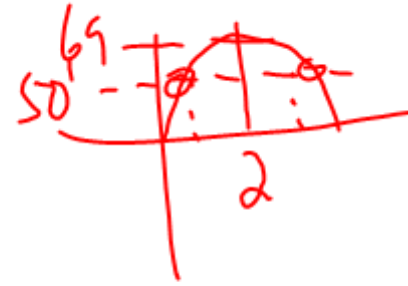
$$t = \frac{-b}{2a} = \frac{-64}{2(-16)} = 2 \text{ seconds}$$

Max height $s(2) = -16(2)^2 + 64(2) + 5 = \underline{69 \text{ ft}}$

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When does the ball reach 50 ft high

$$50 = -16t^2 + 64t + 5$$

$$0 = -16t^2 + 64t - 45$$

$$t = \frac{-(-64) \pm \sqrt{(-64)^2 - 4(-16)(-45)}}{2(-16)} = \begin{matrix} \approx 1.0 \text{ sec} \\ \approx 3.1 \text{ sec} \end{matrix}$$